


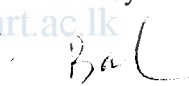
# DECLARATION

I hereby, declare, that the work included in this thesis in part or whole,  
has not been submitted for any other academic qualification at any  
institution.

  
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Thank you

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