# VIRTUAL SUPPPORTS TO ANALYSE STATIC FLOATING STRUCTURES AND DYNAMIC SYSTEMS BY STATIC ANALYSIS SOFTWARE 

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Supervisor
Date

Mr. Kapila Peiris
$\qquad$

Supervisor
Date

Dr. M. Narayana


#### Abstract

When an object with high rigidity is subjected to free forces, moments and constrained forces, moments, stresses and strain will be formed in it. A support may be identified as a constrained which supplies forces/moment without any displacement.

In some cases although the constrains could balance the free forces/moments by and keep the system under equilibrium, the constraints cannot be keep a unique displacement (field). Therefore in such a case in an elemental analysis the solution for displacements will have many solutions conditions and in a computer where numerical methods (iterative) are used such solution will not be possible.

In this study a method is introduced to overcome this problem by the concept of 'virtual constraints' without changing the original stress-strain condition of the system

System without adequate constraints will be known as floating system and dynamic systems (with high rigidity) with the application of reversed inertia forces could also be considered as floating system. Therefore such system also could be analyzed for stress-strain by proper introduction of artificial supports with the same software meant to analyses static system.


Keywords - Virtual supports, Floating system

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Abstract ..... ii
ACKNOWLEDGEMENT ..... iii
List of abbreviations ..... ix

1. INTRODUCTION ..... 1
1.1 Find stress field of a static body ..... 1
1.2 solving stress-strain problems ..... 3
1.2.1 Determining displacement field of no-constrain beam structure ..... 4
1.2.2 Find displacement filed of no-constrain CST plate element ..... 8
1.2.3.Analysis of a simple un-constraints body by computer base FEA package 11
1.2 Objective ..... 16
2. LITEREATURE REVIEW ..... 17
2.1 Studies done on virtual supports ..... 17
2.2 Finite Element Method ..... 22
2.3 Brief History ..... 22
2.4 Computers for FEA ..... 23
2.5 Finite Element and computers ..... 23
2.6 Abaqus as general purpose software ..... 25
2.7 Main steps of Abaqus analysis ..... 25
2.7.1 Discretize the model ..... 25
2.7.2 Element section properties ..... 26
2.7.3 Material data ..... 26
2.7.4 Loads module in Abaqus ..... 26
2.7.4.7 Define pipe pressure load ..... 27
2.8 Define boundary condition in Abaqus ..... 28
2.8.1 XSYMM Symmetry about a plane $\mathrm{X}=$ constant $(\mathrm{U} 1=\mathrm{UR} 2=\mathrm{UR} 3=0)$28
2.8.2 YSYMM Symmetry about a plane $Y=$ constant $(U 2=U R 1=U R 3=0)$28
2.8.3 ZSYMM Symmetry about a plane $\mathrm{Z}=$ constant $(\mathrm{U} 3=\mathrm{UR} 1=\mathrm{UR} 2=0) 28$2.8.4 XASYMM Anti-symmetry about a plane with $\mathrm{X}=$ constant $(\mathrm{U} 2=\mathrm{U} 3=$UR1 = 0)28
2.8.5 YASYMM Anti-symmetry about a plane with $\mathrm{Y}=$ constant $(\mathrm{U} 1=\mathrm{U} 3=$UR2 $=0$ )29
2.8.6 ZASYMM Anti-symmetry about a plane with $\mathrm{Z}=$ constant $(\mathrm{U} 1=\mathrm{U} 2=$UR3 = 0)29
2.8.7 PINNED Pinned $(\mathrm{U} 1=\mathrm{U} 2=\mathrm{U} 3=0)$ ..... 29
2.8.8 ENCASTRE Fully built-in $(\mathrm{U} 1=\mathrm{U} 2=\mathrm{U} 3=\mathrm{UR} 1=\mathrm{UR} 2=\mathrm{UR} 3=0)$ ..... 29
2.8.9 Defining velocity/angular velocity boundary condition ..... 29
2.8.10 Defining acceleration/angular acceleration boundary condition ..... 29
2.9 Depth in to Finite element analysis ..... 29
2.9.1. Discretization and element selection ..... 31
2.9.2 . Selection a displacement function ..... 34
2.9.3. Define the strain/displacement and stress/strain relationship ..... 34
2.9.4. Derive element stiffness matrix and equations ..... 34
2.9.5 Assembly the element equations to obtain the global or total equations ..... 37
2.9.6 solve for the unknown degree of freedom or generalized displacement ..... 40
2.9.7 solve for the element stress and strain ..... 41
2.9.8 Interpret the results ..... 41
2.10 Derivation of the stiffness matrix for a bar element in a local coordinates ..... 41
2.11 Derivation of the constant-strain triangular element stiffness matrix andequation44
2.12 Cofactor method (Adjoining method) to determine the inverse of a matrix ..... 49
2.13 Equation of elasticity ..... 49
2.13.1 differential equation for equilibrium ..... 49
2.13.2 Strain/Displacement and compatibility equations ..... 51
2.13.3 Stress/strain relationship ..... 53
3. INTRODUCTION OF VIRTUAL CONSTRAINTS ..... 55
3.1 Floating structure ..... 55
3.2 identification of floating, non-floating constraints by kinematics method ..... 55
3.3 identification of floating, non-floating constraints by static method ..... 56
3.3.1 Use virtual support to analyses roof structure of Kulasinghe auditorium in nerd center ..... 61
3.4 Analyzing of a dynamic system with virtual supports ..... 69
3.4.1 Analyzing of a rotating disc with virtual supports ..... 70
3.4.1.1 Calculation of centrifugal force and tangential force ..... 71
3.4.2 Stress-strain analysis of a wind blade ..... 80
3.4.2.1 Determine $\boldsymbol{f i}$ from dynamics ..... 81
3.4.2.2 Apply reversed inertia forces at the nodes ..... 84
3.4.2.3 Apply virtual constraints ..... 85
3.4.2.4 Analysis the system ..... 86
3.4.2.5 Reaction Moment around Y axis of Virtual support ..... 87
4. CONCLUSION ..... 88
References ..... 90
Appendix ..... 94

## List of Figures

Figure 1: Stress tensor on an infinitesimal element 1
Figure 2: AB and BC beam structure 4
Figure 3: Nodal forces on the model 4
Figure 4: Nodal displacement on the model 5
Figure 5:Local forces and displacement of elements 5
Figure 6: Displacement vectors of CST elements 8
Figure 7:Schematic diagram of un-constrained beam 11
Figure 8: Error message in Abaqus output 11
Figure 9: Error message in ANSYS output 12
Figure 10: Error message of Nastran solver 12
Figure 11: Error message of FEmap solver 13
Figure 12:error message in Strand7 solver 13
Figure 13: Error message in SolidWorks simulation 14
Figure 14: Rigid foundation with no supports 17
Figure 15: Flow chart followed to get unique thermal stress without DBC s 19
Figure 16: Hydrostatic pressure on the object 20
Figure 17: FE simulation result 20
Figure 18: procedure to remove rigid body motion from deformation result solved without DBCs 21

Figure 19: Line element used in FEA 31
Figure 20: Plate element used in FEA 33
Figure 21: 3D elements used in FEA 33
Figure 22: Axisymmetric elements used in FEA 33
Figure 23:linear spring element 35
Figure 24:virtual displacement applied on the particle 37
Figure 25: Two spring assembly 37
Figure 26: Local displacement of beam 42
Figure 27: Nodal forces applied in local direction 42
Figure 28: displacement in a CST element 44
Figure 29: stress tensors on plane element 49

Figure 30: stress elements in three dimensional case 50
Figure 31: differential element before and after deformation 51
Figure 32: Deformation of 3D element for tensile stress in $x$ direction 53
Figure 33: Virtual supports on a body 57
Figure 34: Roof of Kulasinghe auditorium 61
Figure 35:FEA model of structure 62
Figure 36: Mesh on the model 63
Figure 37: boundary condition on the model 64
Figure 38: Virtual supports on the roof 65
Figure 39: Loading on the structure 66
Figure 40: Von misses stress developed on the structure 67
Figure 41: Reaction force in X direction of virtual constraint 68
Figure 42: Reaction force in Z direction of virtual constraint 68
Figure 43: Reaction Moment around Y axis of virtual constraint 69
Figure 44: Reversed inertia forces on an object 69
Figure 45: Force on a rotating disc 70
Figure 46: Center of gravities of first segment 72
Figure 47: Reverse inertia forces on the disc 74
Figure 48: Boundary condition on the rotating disc 75
Figure 49: virtual supports to the disc 76
Figure 50: Von misses stress of rotating disc 77
Figure 51: Reaction force in X direction of virtual constraint 78
Figure 52:Reaction force in Z direction of virtual constraint 78
Figure 53:Moment around in Z axis of virtual constraint 79
Figure 54:kinematics of wind blade 80
Figure 55: Constraint on wind blade 81
Figure 56: Wind force on the FEA model 82
Figure 57: drag forces on the wind blade 83
Figure 58: reversed inertia forces on the model 84
Figure 59: Virtual support on the model 85
Figure 60: Stress analysis of wind blade at static mode 86
Figure 61: Reaction moment around Y axis of virtual constraint 87
Figure 62:Kinematics on wind blade ..... 94
List of Table
Table 1:Parameters of the rotating disc ..... 71
Table 2: Calculation of inertia forces ..... 73

## List of abbreviations

| FEA | Finite Element Analysis |
| :--- | :--- |
| FEM | Finite Element Method |
| CFD | Computational Fluid Dynamics |
| AMS | Automatic Multi-level Sub structuring eigen solver |
| CAE | Complete Abaqus Environment |
| MPE | Minimum potential Energy theorem |
| CST | Constant Strain Triangular |
| NERD | National Engineering Research and Development Center |
| DBC | Displacement Boundary Condition |

